

Power-Law Scaling of the Impact Crater Size-Frequency Distribution on Pluto: A Preliminary Analysis Based on First Images from New Horizons' Flyby

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The recent (14th July 2015) flyby of NASA's New Horizons spacecraft of the dwarf planet Pluto resulted in the first high-resolution images of the geological surface-features of Pluto. Since previous studies showed that the impact crater size-frequency distribution (SFD) of different celestial objects of our solar system follows power-laws, the aim of the present analysis was to determine, for the first time, the power-law scaling behavior for Pluto's crater SFD based on the first images available in mid-September 2015. The analysis was based on a high-resolution image covering parts of Pluto's regions *Sputnik Planum*, *Al-Idrisi Montes* and *Voyager Terra*. 83 impact craters could be identified in these regions and their diameter (D) was determined. The analysis revealed that the crater diameter SFD shows a statistically significant power-law scaling ($\alpha = 2.4926 \pm 0.3309$) in the interval of D values ranging from 3.75 ± 1.14 km to the largest determined D value in this data set of 37.77 km. The value obtained for the scaling coefficient α is similar to the coefficient determined for the power-law scaling of the crater SFDs from the other celestial objects in our solar system. Further analysis of Pluto's crater SFD is warranted as soon as new images are received from the spacecraft.

1 Introduction

The first close-up images of Pluto from NASA's New Horizons spacecraft, received in mid-September 2015, show a complex surface structure of Pluto never seen before in this detail. During the spacecraft's flyby of Pluto on 14th July 2015, images were taken by New Horizons' Long Range Reconnaissance Imager (LORRI) with a cooled 1024×1024 pixel CCD camera from a distance of approx. 12,500 km making it possible to obtain high-resolution images of Pluto's surface. Due to the slow transmission (about 1–2 Kbps), it will take around 16 months for all flyby images of Pluto to be received in full [1].

Many phenomena in astrophysics follow a power-law, i.e. the relationship between features exhibits a scale-invariance. Examples are the characteristics of the channel network on Mars [2], the relationship between solar flare occurrence and total flare energy [3], the correlation between a supermassive black hole mass and the host-galaxy bulge velocity dispersion ("M-sigma relation") [4], the distribution of initial masses for a population of stars ("initial mass function") [5], Kepler's third law, or the distribution of galaxies in the universe [6–8].

Size-frequency distributions (SFD) of natural objects also follow in general a power-law. Examples are the SFD of fragment sizes due to a fragmentation process [9], the SFD of landslides [10], the particle SFD of volcanic ash [11], the mass distribution objects of the Kuiper belt [12] — or the SFD of impact crater diameters on celestial objects.

Already in 1940 Young showed that the impact crater SFD on the Earth's Moon can be described by two power-laws with different scaling exponents. Further studies extended the analysis to other celestial objects, e.g. Earth [13], Mars

[14–16] and Mercury [17].

Due to the lack of high-resolution images available, it has not been possible until now to analyze the impact crater SFD of Pluto. With the first images now available from NASA's New Horizons mission, the aim of the present paper was to conduct such a first, preliminary, analysis.

2 Materials and methods

2.1 Data

For the present analysis the raw images* obtained by the New Horizons' LORRI as of 14th September 2015 were visually inspected in order to find an image showing impact craters of Pluto with the highest resolution possible. An additional selection criterion was that the image had to be taken by LORRI at an angle capturing the region of interest maximally parallel to the camera, minimizing geometrical distortions of the features in the image.

The image lor_0299174809_0x630_sci_4 (in the following denoted as LOR-0299174809) was selected as fulfilling these criteria (see Figure 1(b)). LOR-0299174809 displays a particular area covering parts of Pluto's regions *Sputnik Planum*, *Al-Idrisi Montes* and *Voyager Terra*. The image was taken by LORRI on 14th July 2015, 10:14:50 UTC, with an exposure time of 150 ms.

2.2 Determination of crater diameter values

The image LOR-0299174809 was analyzed in Adobe Illustrator (version CS5; Adobe Systems, CA, USA) by first visually

*LORRI Images from the Pluto Encounter, <http://pluto.jhuapl.edu/soc/Pluto-Encounter>

identifying the craters on the image and measuring their diameters (D). The obtained values were then rescaled to give the final values in the unit km. To do so, the information given on NASA's website* was used. Information on the website indicated that image number three (from top), which covers the region displayed in LOR-0299174809, is 470 km in width.

2.3 Statistical analysis

For the statistical analysis we used the mathematical framework provided by the Santa Fe Institute [18, 19]. The data were analyzed in Matlab (version 2010a; Mathworks Inc., Natick, MA, USA).

2.3.1 Estimation of the lower-bound and exponent of the power-law model

A quantity x shows power-law scaling if it stems from a probability distribution $p(x) \sim x^{-\alpha}$, with the exponent α defining the characteristics of the scaling. To test if an empirically obtained probability distribution follows a power-law, classically a histogram is calculated and the distribution is analyzed on a doubly logarithmic plot. Since $p(x) \sim \alpha \ln(x) + \text{const.}$, a power-law distributed quantity x follows a straight line in the plot. Besides the fact that this method was (and is still) used to investigate power-law scaling of different quantities this approach can generate significant systematic errors [18]. Therefore, for the present analysis we used a framework presented by Clauset et al. [18] that circumvents these errors and also offers the possibility of estimating the lower bound of the power-law (x_{\min}). The determination of x_{\min} is crucial when analyzing empirical data for power-law scaling since often the power-law behavior applies only for the tail region of the distribution, i.e. for values greater than the threshold value x_{\min} .

For the obtained crater diameter (D) data ($= x$) the power-law threshold value D_{\min} ($= x_{\min}$) was determined based on the method described by Clauset et al. [18] which uses the Kolmogorow-Smirnov (KS) statistics. The scaling exponent α was then calculated with a maximum likelihood fitting method also described by Clauset et al. [18].

2.3.2 Determination of the statistical significance of the power-law fit

In order to determine if the fitted power-law can be considered statistically significant, a goodness-of-fit test described by Clauset et al. [18] was employed. To this end, power-law distributed synthetic data was generated with values of α and x_{\min} that are equal to the values obtained by fitting the empirical data to the power-law model. Each synthetic data set is then fitted to the model and the KS statistics determined. Based on the occurrences of times the KS statistic is larger

than for the empirical values, a p -value is calculated. For $p < 0.1$ the fit of the power-law model to the empirical data is considered to be statistically not significant, i.e. it can be ruled out that the empirical distribution obeys a power-law scaling. Thus, the p -value in this case represents a measure of the hypothesis that is tested for validity. A high value of p corresponds to a good fit.

3 Results, discussion and conclusion

83 impact craters could be identified and their diameter values were determined, ranging from 0.84 km to 37.77 km. Using the obtained 83 D values and the methods described in Section 2.3.1, the scaling coefficient α was determined to be $\alpha = -2.4926 \pm 0.3309$ and the scaling threshold value to be $D_{\min} = 3.75 \pm 1.14$ km. Thus, for D in the range $[3.75 \pm 1.14 \text{ km}, 37.77 \text{ km}]$ the values follow a power-law. The log-likelihood (L) of the data $D \geq D_{\min}$ under the fitted power law was determined to be $L = 104.5688$.

The statistical test, as described in Section 2.3.2, employing 10,000 synthetic data sets revealed a p value of 0.2241. Thus, according to the test the hypothesis cannot be refuted that the data follows a power-law, i.e. Pluto's crater SFD shows a power-law scaling. Figure 1(c) visualizes the power-law behavior of the crater SFD.

How do the results of the presented analysis relate to the findings about characteristics of the crater SFD of other celestial objects? As mentioned in the introduction, it well established that the crater SFD of all investigated celestial bodies in our solar system exhibit a power-law scaling.

For example, according to an analysis performed by Robertson and Grieve from 1975 the crater SFD of the Earth is characterized by $\alpha \approx -2$ (for $D \geq 8$ km) [13]. An own analysis using the updated data of impact craters on Earth ($n = 188$) based on the Earth Impact Database[†] revealed $\alpha = 2.0286$ (for $D \geq 7$ km). The Earth Moon's crater SFD has been intensively investigated since the 1940's when Young [20] initially showed that for large D the crater SFD follows a power-law with $\alpha = -3$, and for small D the scaling is described by $\alpha = -1.5$. Subsequent studies described the scaling with laws governed by $\alpha = 2$ (for $D = [\sim 2 \text{ km}, 70 \text{ km}]$) [21], as well as $\alpha = -2$ (for $D < 100$ m) and $\alpha = -2.93$ (for $D > \text{a few } 100 \text{ m}$) [22], for example. Further studies showed that the scaling-relations of the lunar crater SFD need to include the observation that multiple power-laws are necessary to describe the whole SFD spectrum, i.e. α depends on D [23, 24]. A solution for optimally fitting the crater SFD was described based on the idea of using a polynomial function to fit the SFD data in the log-log space, i.e. it could be shown that a polynomial function of 7th degree fit the data well for $D = [300 \text{ m}, 20 \text{ km}]$. The polynomial function included an extra term accounting for the fact that the scaling function also depends on the geological charac-

*<http://tinyurl.com/n9k5mmc>

[†]<http://www.passc.net/EarthImpactDatabase>

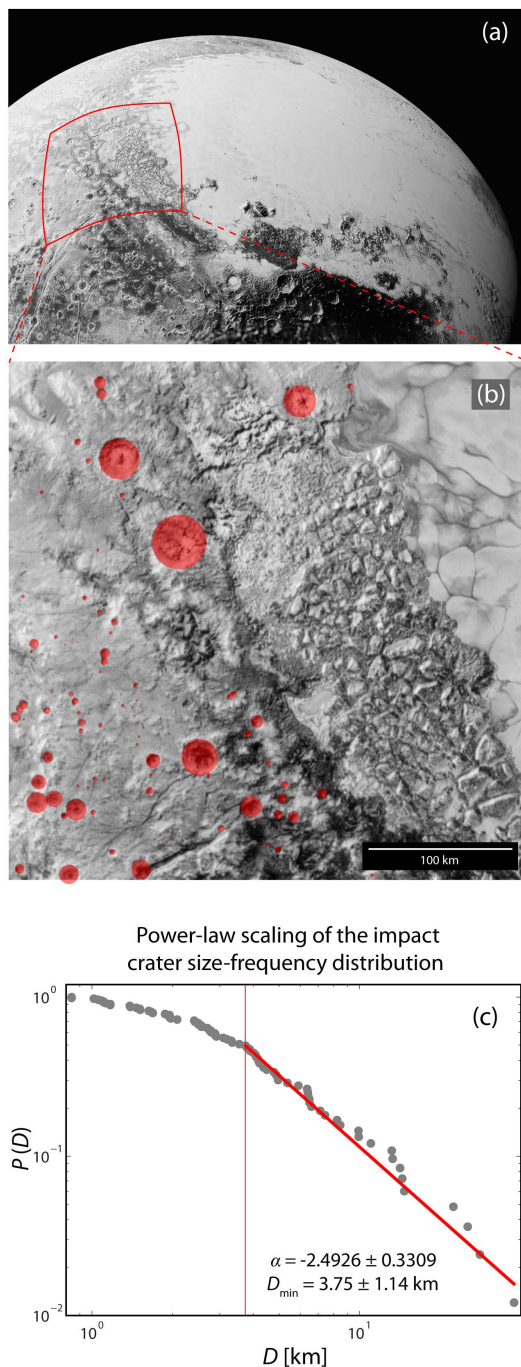


Fig. 1: (a) View of Pluto taken in July 2015 by LORRI on board NASA's New Horizons spacecraft. In the field of view the western lobe of the Tombaugh region is depicted. (b) LORI image lor0299174809_0x630_sci_4 showing a particular area covering parts of Pluto's regions *Sputnik Planum*, *Al-Idrisi Montes* and *Voyager Terra*. (c) Visualization of the power-law scaling of the impact crater size distribution. $P(D)$: complementary cumulative distribution function; D : crater diameter. Images (a) and (b) were obtained from NASA, Johns Hopkins University Applied Physics Laboratory, Southwest Research Institute.

teristics of the region investigated — a finding also made by other studies (e.g., [24–26]). For an extended range of D , in later work a 11th degree polynomial function was published by Neukum [27] valid for $D = [10 \text{ m}, 300 \text{ km}]$ and covering scaling exponents in the range of $\alpha = [-1, 4]$. For the Martian satellites Phobos and Deimos, the crater SFD was determined as being described by a power-law with $\alpha \approx 1.9$ for $D = [44 \text{ m}, 10 \text{ km}]$ [16].

Thus, the finding of the present analysis concerning the power-law characteristics (i.e., $\alpha = 2.4926 \pm 0.3309$ for $D = [3.75 \pm 1.14 \text{ km}, 37.77 \text{ km}]$) of the crater SFD of Pluto is comparable to the power-laws observed for the other celestial bodies. That Pluto's diameter scaling for $D < 3.75 \pm 1.14 \text{ km}$ does not follow the $\alpha = -2.4926$ scaling relies most probably on the fact that small craters are much faster deteriorated due to erosion and that counting of craters with small D was not perfectly possible due to the limited resolution of the available image. The lowest D value ($3.75 \pm 1.14 \text{ km}$) for which the power law holds might interpreted as related to a transition from simple to complex craters. Interestingly, such a “transition diameter” was predicted for Pluto to be in the range of 4–5 km [28–30].

This analysis, of course, should be regarded only as a preliminary study for further follow-up as soon as the full set of images from Pluto is available and the images have been processed to deliver a high-resolution picture of Pluto's surface morphology. A limitation of the present analysis is that only one high-resolution image with sufficient craters was available. It was therefore only possible to obtain a relatively low number of crater diameter values ($n = 83$).

Knowledge of Pluto's crater SPF will not only give insights in the universality of the crater SFD scaling relations but necessarily will also help in the understanding of the history of Pluto and the characteristics of the Kuiper belt which Pluto is part of.

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